

JEE Main (Phase-II) 2020

Memory Based Questions & Solutions

SUBJECT

MATHEMATICS

Date: 04 September, 2020 (Shift-1)

Time: 9 AM to 12 PM

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1. In a group 63% people read news paper A while 76% people read news paper B. If $x\%$ people read both A and B then x may be
 (1) 37% (2) 68% (3) 29% (4) 55%
 Ans. (4)

Sol. $n(A) = 63\%$

$n(B) = 76\%$

$n(A \cap B) = x\%$

Let $n(A \cup B) = 100$

$n(A) = 63, n(B) = 76, n(A \cap B) = x$

$n(A \cup B) = n(A) + n(B) - n(A \cap B) \leq 100$

$63 + 76 - x \leq 100$

$x \geq 39$

but $n(A \cap B) \leq n(A) \therefore 39 \leq x \leq 63$

2. If $\int \frac{\sqrt{x}}{(1+x)^2} dx$, then find the value of $f(3) - f(1)$

(1) $\frac{\pi}{12} + \frac{1}{2} + \frac{\sqrt{3}}{4}$

(2) $\frac{\pi}{12} + \frac{1}{2} - \frac{\sqrt{3}}{4}$

(3) $\frac{\pi}{12} + \frac{1}{3} - \frac{\sqrt{3}}{4}$

(4) $\frac{\pi}{12} + \frac{1}{4} - \frac{\sqrt{3}}{4}$

- Ans. (2)

Sol. $f(x) = \int \frac{\sqrt{x}}{(1+x)^2} dx$

Let $x = \tan^2 \theta$

$dx = 2 \tan \theta \sec^2 \theta d\theta$

$f(x) = \int \frac{\tan \theta}{(\sec^2 \theta)^2} \cdot 2 \tan \theta \sec^2 \theta d\theta$

$f(x) = \int \frac{\tan \theta}{\sec^4 \theta} \cdot 2 \tan \theta \sec^2 \theta d\theta$

$f(x) = \int 2 \tan^2 \theta \cos^2 \theta d\theta$

$f(x) = \int 2 \sin^2 \theta d\theta$

$f(x) = \int (1 - \cos 2\theta) d\theta$

$f(x) = \theta - \frac{\sin 2\theta}{2} + C = \theta - \frac{\tan \theta}{1 + \tan^2 \theta} + C$

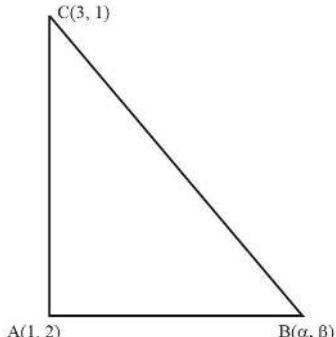
$f(x) = \tan^{-1} \sqrt{x} - \frac{\sqrt{x}}{1+x} + C$

now $f(3) - f(1) = \tan^{-1} \sqrt{3} - \frac{\sqrt{3}}{1+3} - \tan^{-1} \sqrt{1} + \frac{1}{1+1}$

$= \frac{\pi}{3} - \frac{\pi}{4} + \frac{1}{2} - \frac{\sqrt{3}}{4} = \frac{\pi}{4} + \frac{1}{2} - \frac{\sqrt{3}}{4}$

3. Let ΔABC is a right angled triangle right angled at A such that $A(1, 2)$, $C(3, 1)$ and area of $\Delta ABC = 5\sqrt{5}$ then abscissa of B can be
- (1) $1+5\sqrt{2}$ (2) $1+2\sqrt{5}$ (3) $1-5\sqrt{2}$ (4) $3+2\sqrt{5}$
- Ans. (2)

Sol.



$$m_{AB} = \frac{\beta - 2}{\alpha - 1}$$

$$m_{AC} = \frac{2 - 1}{1 - 3} = -\frac{1}{2}$$

$$AB \perp AC \quad \therefore \quad \frac{\beta - 2}{\alpha - 1} \left(-\frac{1}{2} \right) = -1$$

$$\beta = 2\alpha - 2 + 2 \quad \Rightarrow \quad \beta = 2\alpha$$

$$\text{Now area of } \Delta ABC = 5\sqrt{5} = \frac{1}{2} AB \cdot AC$$

$$\Rightarrow \frac{1}{2} \sqrt{(3-1)^2 + (1-2)^2} \cdot \sqrt{(\alpha-1)^2 + (\beta-2)^2} = 5\sqrt{5}$$

$$\Rightarrow \sqrt{(\alpha-1)^2 + (2\alpha-2)^2} = 10$$

$$\Rightarrow \sqrt{(\alpha-1)^2} \sqrt{5} = 5 \quad \Rightarrow \quad |\alpha-1| = 2\sqrt{5} \quad \Rightarrow \quad \alpha = 1 \pm 2\sqrt{5}$$

4. Let $f(x) = |x - 2|$ and $g(x) = f(f(x))$, $x \in [0, 4]$, then $\int_0^3 (g(x) - f(x)) dx =$

- (a) 1 (b) 2 (3) 3 (4) 4
Ans. (1)

Sol. $f(x) = |x - 2| = \begin{cases} 2 - x & x < 2 \\ x - 2 & x \geq 2 \end{cases}$

$$g(x) = f(f(x)) = \begin{cases} 2 - f(x) & f(x) < 2 \\ f(x) - 2 & f(x) \geq 2 \end{cases}$$

$$= \begin{cases} 2 - (2 - x) & 2 - x < 2, \quad x < 2 \\ (2 - x) - 2 & 2 - x \geq 2, \quad x < 2 \\ 2 - (x - 2) & x - 2 < 2, \quad x \geq 2 \\ (x - 2) - 2 & x - 2 \geq 2, \quad x \geq 2 \end{cases}$$

$$= \begin{cases} x & 0 < x < 2 \\ -x & x \leq 0 \\ 4-x & 2 < x < 4 \\ x-4 & x \geq 4 \end{cases}$$

$$\int_0^3 (g)(x) - f(x) dx = \int_0^2 x dx + \int_2^3 (4-x) dx - \int_0^3 |x-2| dx = 1$$

5. $\sum_{r=0}^{20} {}^{50-r}C_6 =$
 (1) ${}^{54}C_7 - {}^{30}C_6$ (2) ${}^{51}C_6 - {}^{30}C_6$ (3) ${}^{51}C_7 - {}^{30}C_6$ (4) ${}^{51}C_7 - {}^{30}C_7$
 Ans. (3)

Sol. $\sum_{r=0}^{20} {}^{50-r}C_6 =$
 ${}^{50}C_6 + {}^{49}C_6 + {}^{48}C_6 + {}^{47}C_6 + \dots + {}^{30}C_6$
 $= {}^{50}C_6 + {}^{49}C_6 + {}^{48}C_6 + {}^{47}C_6 + \dots + {}^{30}C_6 + {}^{30}C_7 - {}^{30}C_7$
 $= {}^{51}C_7 - {}^{30}C_7$

6. Let $x \frac{dy}{dx} - y = x^2 (x \cos x + \sin x)$ is a differential equation. If $(\pi) = \pi$ then $f''\left(\frac{\pi}{2}\right) + f\left(\frac{\pi}{2}\right) =$
 (1) $\frac{\pi}{2} + 2$ (2) $\frac{\pi}{2} - 2$ (3) $\frac{\pi}{2} + 1$ (4) $\frac{\pi}{2} - 1$
 Ans. (1)

Sol. Given $x \frac{dy}{dx} - y = x^2 (x \cos x + \sin x)$

$$\Rightarrow \frac{dy}{dx} - \frac{1}{x}y = x(x \cos x + \sin x) \quad \therefore \text{I.F.} = e^{\int \frac{-1}{x} dx} = e^{-\ln x} = \frac{1}{x}$$

$$\therefore \text{solution is } y \cdot \frac{1}{x} = \int \frac{1}{x} \cdot x(x \cos x + \sin x) dx + C$$

$$\frac{y}{x} = \int (x \cos x + \sin x) dx + C \quad \Rightarrow C = 1$$

$$y = x^2 \sin x + x$$

$$\frac{dy}{dx} = x^2 \cos x + 2x \sin x + 1$$

$$\frac{d^2y}{dx^2} = -x^2 \sin x + 2x \cos x + 2x \cos x + 2 \sin x = -x^2 \sin x + 4x \cos x + 2 \sin x$$

$$\therefore f''\left(\frac{\pi}{2}\right) + f\left(\frac{\pi}{2}\right) = \left(-\frac{\pi^2}{4} + 4.0 + 2\right) + \left(\frac{\pi^2}{4} \cdot 1 + \frac{\pi}{2}\right)$$

$$\therefore \frac{\pi^2}{4} + 2 + \frac{\pi^2}{4} + \frac{\pi}{2} = \frac{\pi}{2} + 2$$

7. Let $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ be an ellipse such that $LR = 10$ and its eccentricity is equal to maximum value of

$$\text{quadratic expression } f(t) = \frac{5}{12} + t - t^2 \text{ then } (a^2 + b^2) =$$

Ans. 126

$$\text{Sol. } LR = \frac{2b^2}{a} = 10 \Rightarrow b^2 = 5a$$

$$f(t) = \frac{5}{12} - \left(t^2 - t + \frac{1}{4} - \frac{1}{4}\right) = \frac{5}{12} + \frac{1}{4} - \left(t - \frac{1}{2}\right)^2$$

$$= \frac{2}{3} - \left(t - \frac{1}{2}\right)^2$$

$$\max f(t) = \frac{2}{3} = e$$

$$b^2 = a^2(1 - e^2)$$

$$5a = a^2 \left(1 - \frac{4}{9}\right) \Rightarrow 5 = \frac{5}{9}a \Rightarrow a^2 = 81, b^2 = 45$$

$$a^2 + b^2 = 126$$

8. If α, β are roots of $x^2 - 3x + p = 0$ and γ, δ are roots of $x^2 - 6x + q = 0$ and $\alpha, \beta, \gamma, \delta$ are in increasing

geometric progression then value of $\frac{2q+p}{2q-p}$ is equal to

$$(1) \frac{7}{9}$$

$$(2) -\frac{7}{9}$$

$$(3) \frac{9}{7}$$

$$(4) -\frac{9}{7}$$

Ans. (3)

$$\text{Sol. } \alpha = a, \beta = ar, \gamma = ar^2, \delta = ar^3$$

$$\alpha = \beta = 3 \Rightarrow a + ar = 3 \dots \dots \dots (1)$$

$$\gamma + \delta = 6 \Rightarrow ar^2 + ar^3 = 6 \dots \dots \dots (2)$$

$$\text{By (1) and (2)} \Rightarrow \frac{ar^2(1+r)}{a(1+r)} = \frac{6}{3} \Rightarrow r^2 = 2$$

$$\Rightarrow r = \sqrt{2}$$

$$\therefore \frac{2q+p}{2q-p} = \frac{9}{7}$$

9. The mean and variance of 5, 7, 12, 10, 15, 14, a, b are 10 and 13.5 respectively then value of $|a - b| =$

$$(1) 5$$

$$(2) 6$$

$$(3) 7$$

$$(4) 8$$

Ans. (3)

$$\text{Sol. } \frac{5+7+12+10+15+14+a+b}{8} = 10$$

$$\Rightarrow 63 + a + b = 80 \Rightarrow a + b = 17 \dots \dots \dots (1)$$

$$\sigma^2 = \frac{\sum x_i^2}{n} - \left(\frac{\sum x_i}{n} \right)^2$$

$$\Rightarrow 13.5 = \frac{25 + 49 + 144 + 100 + 225 + 196 + 1^2 + b^2}{8} - 100$$

$$908 = a^2 + b^2 + 739$$

$$a^2 + b^2 = 169$$

$$(a+b)^2 - 2ab = 169$$

$$289 - 169 = 2ab \Rightarrow ab = 60$$

$$\therefore |a-b|^2 = (a+b)^2 - 4ab = 289 - 240 = 49$$

$$\therefore |a-b| = 7$$

10. If $1 + (1 - 2^2 \cdot 1) + (1 - 4^2 \cdot 3) + (1 - 6^2 \cdot 5) + \dots + (1 - 20^2 \cdot 19) = \alpha - 220\beta$ then $(\alpha, \beta) =$
 (1) (11, 97) (2) (11, 103) (3) (10, 97) (4) (10, 103)

Ans. (2)

Sol. $S = 1 + \sum_{r=1}^{10} 1 - (2r)^2 (2r-1) = 1 + 10 - \sum_{r=1}^{10} (8r^3 - 4r^2) = 11 - \left[8 \left(\frac{10 \times 11}{2} \right)^2 - 4 \cdot \left(\frac{10 \times 11 \times 21}{6} \right) \right]$
 $= 11 - [2(110)^2 - 140 \times 11]$
 $= 11 - 22(1100 - 70)$
 $= 11 - 220(110 - 7)$
 $\therefore \alpha = 220\beta$
 $= 11 - 220(103)$
 $\therefore \alpha = 11, \beta = 103$
 $(\alpha, \beta) = 11, 103$

11. For equation $[x]^2 + 2[x+2] - 7 = 0$, $x \in \mathbb{R}$ number of solution of equation is/are
 (1) four integer solution (2) infinite solution (3) No solution (4) two solution

Ans. (2)

Sol. $[x]^2 + 2[x+2] - 7 = 0$

$$[x]^2 + 2([x]+2) - 7 = 0$$

$$\text{Let } [x] = t$$

$$t^2 + 2t - 3 = 0$$

$$t = 1, -3$$

$$[x] = -3, 1$$

$$x \in [-3, -2) \cup [1, 2]$$

Hence infinite solution

12. Integration: $\int \frac{x^2 dx}{(x \sin x + \cos x)^2}$ is equal to

$$(1) \frac{\sin x + x \cos x}{x \sin x + \cos x} + C \quad (2) \frac{\sin x + x \cos x}{x \sin x - \cos x} + C \quad (3) \frac{x \cos - \sin x}{\cos x - x \sin x} + C \quad (4) \frac{\sin x - x \cos x}{x \sin x + \cos x} + C$$

Ans. (4)

Sol. $\int \frac{x^2 dx}{(x \sin x + \cos x)^2} = \int \frac{x}{\cos x} \cdot \frac{x \cos x}{(x \sin x + \cos x)^2} dx$

$$= \frac{x}{\cos x} \int \frac{x \cos x}{(x \sin x + \cos x)^2} dx - \int \left[\frac{d}{dx} (x \sec x) \int \frac{x \cos x}{(x \sin x + \cos x)^2} dx \right] dx$$

$$= \frac{x}{\cos x} \left(-\frac{1}{x \sin x + \cos x} \right) + \int \sec^2 x \, dx$$

$$\therefore \int \frac{x \cos x}{(x \sin x + \cos x)^2} dx = \frac{-1}{x \sin x + \cos x} \text{ and}$$

$$\frac{d}{dx} (x \sec x) = \sec x + \sec x \tan x = \sec x \left(1 + \frac{x \sin x}{\cos x} \right) = \sec^2 x (x \sin x + \cos x)$$

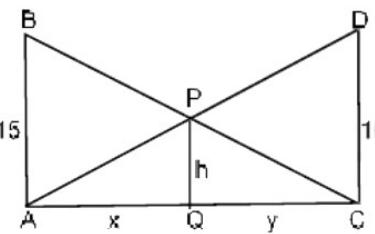
$$= \frac{-x}{\cos x (x \sin x + \cos x)} + \frac{\sin x}{\cos x} + c$$

$$= \frac{-x + x \sin^2 x + \sin x \cos x}{\cos x (x \sin x + \cos x)} = \frac{\sin x - x \cos x}{x \sin x + \cos x} + c$$

13. Two poles AB and CD of height 15 m and 10 m respectively. A and C are on level ground. Point of intersection of AD and BC is P then height of P is

Ans. 6

Sol.



$$\Delta AQP \sim \Delta ACD \Rightarrow \frac{x}{h} = \frac{x+y}{10} \quad \dots\dots(1)$$

$$\therefore \Delta CQP \sim \Delta CAB \Rightarrow \frac{y}{h} = \frac{x+y}{15} \quad \dots\dots(2)$$

$$(1) + (2) \rightarrow \frac{x+y}{h} = (x+y) \left(\frac{1}{10} + \frac{1}{15} \right) \Rightarrow h = 6$$

14. Consider two statements

S₁: $\sim p \rightarrow (\sim q \leftrightarrow \sim p)$ is a tautology

S₂: $(\sim q \wedge p) \rightarrow q$ is a fallacy then

(1) Statement I is true, statement II is false

(2) Statement I is false, statement II is true

(3) Both true

(4) Both false

Ans. (4)

Sol. I: $\sim p \rightarrow (\sim q \leftrightarrow \sim p)$

p	q	$\sim p$	$\sim q$	$\sim q \leftrightarrow \sim p$	$\sim p \rightarrow (\sim q \leftrightarrow \sim p)$	$\overset{(I)}{p \wedge \sim q}$	$(\sim q \wedge p) \rightarrow q$
T	T	F	F	T	T	F	T
T	F	F	T	F	T	T	F
F	T	T	F	F	F	F	T
F	F	T	T	T	T	F	T

both are false

15. If $u = \frac{2z+i}{z-ki}$ where $z = x + iy$ and $k > 0$ curve $\operatorname{Re}(u) + \operatorname{Im}(u) = 1$ cuts y-axis at two points P and Q such that $PQ = 5$ then value of k is
 (1) 1 (2) 2 (3) 3 (4) 4
 Ans. (2)

Sol. $u = \frac{2(x+iy)+i}{(x+iy)-ki} = \frac{2x+(2y+1)i}{x+(y-k)i} \times \frac{x-(y-k)i}{x-(y-k)i}$

$$\text{Real part of } u = \operatorname{Re}(u) = \frac{2x^2 + (2y+1)(y-k)}{x^2 + (y-k)^2}$$

$$\text{Imaginary part of } u = \operatorname{Im}(u) = \frac{x(2y+1) - 2x(y-k)}{x^2 + (y-k)^2}$$

$$\text{Now } \operatorname{Re}(u) + \operatorname{Im}(u) = 1$$

$$= \frac{2x^2 + (2y+1)(y-k) + x(2y+1 - 2x(y-k))}{x^2 + (y-k)^2} = 1$$

$$\text{for y-axis put } x=0 \Rightarrow \frac{(2y+1)(y-k)}{(y-k)^2} = 1$$

$$\Rightarrow (2y+1)(y-k) = (y-k)^2$$

$$\Rightarrow (y-k)(y+(1+k)) = 0$$

$$y = k, -(1+k)$$

$$\text{Now point P}(0, k), Q(0, -(1+k))$$

$$PQ = |2k+1| = 5$$

$$2k+1 = \pm 5$$

$$2k = 4, -6$$

$$k = 2, -3$$

$$\text{hence } k = 2 \quad (k > 0)$$

16. Probability of hitting a target is $\frac{1}{10}$ then find the minimum number of trials so that probability of at least one success is greater than $\frac{1}{4}$ is

Ans. (3)

Sol. $p = \frac{1}{10}, q = \frac{9}{10}$

$$\therefore p(\text{at least one hit}) = 1 - \left(\frac{9}{10}\right)^n \geq \frac{1}{4}$$

$$\Rightarrow \left(\frac{9}{10}\right)^n \geq \frac{3}{4}$$

$$(0.9)^n \leq .75$$

$$n = 3 \Rightarrow 0.729 \leq .75 \text{ which is true}$$

17. Let $A = \begin{bmatrix} \cos & \text{is in } \theta \\ \text{is in } \theta \cos \theta & \end{bmatrix}, 0 < \theta < \frac{\pi}{24}$ and $A^5 = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$ then which statement is false

- (1) $a^2 - b^2 = \frac{1}{2}$ (2) $a^2 + b^2 \in (0,1)$ (3) $a^2 - d^2 = 0$ (4) $a^2 - c^2 = 1$

Ans. (1)

$$\text{Sol. } A^2 = \begin{bmatrix} \cos \theta & \text{is in } \theta \\ \text{is in } \theta \cos \theta & \end{bmatrix} \begin{bmatrix} \cos \theta & \text{is in } \theta \\ \text{is in } \theta \cos \theta & \end{bmatrix} = \begin{bmatrix} \cos^2 \theta - \sin^2 \theta & 2\text{i sin } \theta \cos \theta \\ 2\text{i sin } \theta \cos \theta & \cos^2 \theta - \sin^2 \theta \end{bmatrix} = \begin{bmatrix} \cos 2\theta & \text{is in } 2\theta \\ \text{is in } 2\theta & \cos 2\theta \end{bmatrix}$$

$$A^3 = \begin{bmatrix} \cos 2\theta & \text{is in } 2\theta \\ \text{is in } 2\theta & \cos 2\theta \end{bmatrix} \begin{bmatrix} \cos \theta & \text{is in } \theta \\ \text{is in } \theta \cos \theta & \end{bmatrix} \\ = \begin{bmatrix} \cos 3\theta & \text{is in } 3\theta \\ \text{is in } 3\theta & \cos 3\theta \end{bmatrix}$$

$$\therefore A^5 = \begin{bmatrix} \cos 5\theta & \text{is in } 5\theta \\ \text{is in } 5\theta & \cos 5\theta \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

$$a = \cos 5\theta, b = \text{is in } 5\theta, c = \text{i sin } 5\theta, d = \cos 5\theta$$

$$a = d, b = c$$

$$(1) a^2 + b^2 = \cos^2 5\theta - \sin^2 5\theta = 1$$

$$(2) a^2 + b^2 = \cos^2 5\theta - \sin^2 5\theta = \cos 10\theta \in (0,1) \text{ as } 0 < \theta < \frac{\pi}{24}$$

$$(3) a^2 - d^2 = 0$$

$$(4) a^2 - c^2 = a^2 - b^2 = 1$$

18. If $(a - \sqrt{2}b \cos x)(a + \sqrt{2}b \cos y) = a^2 - b^2$ then value of $\frac{dy}{dx}$ at $\left(\frac{\pi}{4}, \frac{\pi}{4}\right)$ is-

$$(1) \frac{a-b}{a+b}$$

$$(2) \frac{a+b}{a-b}$$

$$(3) \frac{2a+b}{a-b}$$

$$(4) \frac{2a+b}{a-b}$$

Ans. (2)

$$\text{Sol. } (a - \sqrt{2}b \cos x)(-\sqrt{2}b \sin y) \frac{dy}{dx} + \sqrt{2}b \sin x (a + \sqrt{2}b \cos y) = 0$$

$$\frac{dy}{dx} = \frac{\sqrt{2}b \sin x (a + \sqrt{2}b \cos y)}{\sqrt{2}b \sin y (a - \sqrt{2}b \cos x)} = \frac{\sin x (a + \sqrt{2}b \cos y)}{\sin y (a - \sqrt{2}b \cos x)}$$

$$\frac{dy}{dx} \left(\frac{\pi}{4}, \frac{\pi}{4} \right) = \frac{a+b}{a-b}$$

19. $f(x+y) = f(x) + f(y) + xy^2 + x^2y$ and $\lim_{x \rightarrow 0} \frac{f(x)}{x} = 1$, then find value of $f'(3)$

Ans. 10

$$\text{Sol. } f(x+y) = f(x) + f(y) + xy^2 + x^2y$$

$$f'(x+y) = f'(x) + 0 + y^2 + 2xy$$

$$\text{put } y = -x$$

$$f'(0) = f'(x) + x^2 - 2x^2$$

$$1 = f'(x) - x^2$$

$$f'(x) = 1 + x^2$$

$$f'(3) = 10$$

20. If f is twice differentiable function for $x \in \mathbb{R}$ such that $f(2)=5$, $f'(2)=8$ and $f'(x) \geq 1$, $f''(x) \geq 4$ then
 (1) $f(5)+f'(5) \leq 26$ (2) $f(5)+f'(5) \geq 28$ (3) $f(5)+f'(5) \leq 28$ (4) none of these
 Ans. (2)

Sol. Given $f'(x) \geq 1 \Rightarrow \int_2^5 f'(x) dx \geq \int_2^5 1 dx$
 $\Rightarrow (f(x))_2^5 \geq (x)_2^5 \Rightarrow (f(x))_2^5 \geq (x)_2^5 \Rightarrow f(5) \geq 8 \dots\dots\dots(1)$

Now $\Rightarrow f''(x) \geq 4 \Rightarrow \int_2^5 f''(x) dx \geq \int_2^5 4 dx$
 $= (f'(x))_2^5 \geq (4x)_2^5$
 $\Rightarrow (f'(5)) - (f'(2)) \geq 12$
 $\Rightarrow (f'(5)) \geq 20 \dots\dots\dots(2)$
 $(1) + (2) \Rightarrow f(5) + (f'(5)) \geq 28$

21. If $(2x^2 + 3x + 4)^{10} = \sum_{r=0}^{20} a_r x^r$, then $\frac{a_7}{a_{13}} =$

Ans. 8

Sol. General term $\frac{10}{r_1!r_2!r_3!}(2x^2)^{r_1} \cdot (3x)^{r_2} \cdot (4)^{r_3}$
 $a_7 = \frac{10!2^3 \cdot 3 \cdot 4^6}{3!1!6!} + \frac{10!2^3 \cdot 3^3 \cdot 4^5}{2!3!5!} + \frac{10!2 \cdot 3^5 \cdot 4^4}{1!5!4!} + \frac{10! \cdot 3^7 \cdot 4^3}{7!3!}$
 $a_{13} = \frac{10!2^6 \cdot 3 \cdot 4^3}{6!1!3!} + \frac{10!2^5 \cdot 3^3 \cdot 4^2}{5!3!2!} + \frac{10!2^4 \cdot 3^5 \cdot 4^1}{4!5!1!} + \frac{10! \cdot 2^3 \cdot 3^7 \cdot 4^0}{3!7!}$
 $\frac{a_7}{a_{13}} = \frac{2^3}{2^3} = 8$

22. If from a point $(3,3)$ on the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ a normal is drawn which cuts x axis at $(9,0)$ then value of (a^2, e^2) is

- (1) $\left(\frac{9}{2}, 3\right)$ (2) $\left(\frac{9}{2}, 1\right)$ (3) $(9, 3)$ (4) $(3, 9)$

Ans. (1)

Sol. Hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$

$P(3, 3)$ lies on hyperbola then $\frac{1}{a^2} - \frac{1}{b^2} = \frac{1}{9} \dots\dots\dots(1)$

Normal at $(3, 3)$ is

$$\frac{a^2 x}{3} + \frac{b^2 x}{3} = a^2 + b^2 \quad \text{pass through } (9, 0) \quad 3a^2 = a^2 + b^2 = 2a^2 = b^2$$

$$\text{then } \frac{1}{a^2} - \frac{1}{2a^2} = \frac{1}{9} \quad 2a^2 = 9 \Rightarrow a^2 = \frac{9}{2} \text{ and } b^2 = 9 \quad e^2 = 1 + \frac{b^2}{a^2} = 1 + 2 = 3$$

JEE Main - 2020

Best Result in U.P.



**Aditya Pandey
Percentile
99.936
City Topper**

Application No. 200310320565
DOB - 23-12-2002

65 Students Above 99 Percentile

145 Students Above 98 Percentile

208 Students Above 97 Percentile



Abdullah
(99.92)



Umayr
(99.92)



Shivang Pandey
(99.91)



Vinod Meena
(99.89)



Jnaneswar Rao
(99.89)



Pranav Rastogi
(99.88)



Shiva Kumar
(99.87)



Akshay Verma
(99.86)



Neeraj Gartia
(99.86)



Ayush Kumar
(99.85)



Krishna Bhardwaj
(99.85)



Ganesh
(99.78)



Prashant Singh
(99.74)



Adarsh Goyal
(99.71)



Naman Dhingra
(99.69)



Faraz Siddiqui
(99.68)



Abhishek Kumar
(99.66)



Avinesh Pratap
(99.66)



Ajit Kumar
(99.59)



Gitarththa Bharadwaj
(99.58)



Sameed
(99.58)



Sameer
(99.56)



Abhishek Kumar
(99.54)



Ayush Jaiswal
(99.52)



Sanjay Pratap
(99.52)



Suryanshu Kumar
(99.52)



Mihir Agarwal
(99.50)



Mohil
(99.49)



Brijesh Kumar
(99.48)



Harshit Mishra
(99.47)



Harsh Ghandhani
(99.46)



Abdul Nasir
(99.43)



Vinay Kumar
(99.42)



Rustum Naryaan
(99.42)



Tejewar Reddy
(99.39)



Pruthvi Raj
(99.39)



Debdut Saini
(99.38)



G Sai Kiran
(99.37)



Sahil Kumar
(99.32)



Pankaj
(99.31)



Satyam Agarwal
(99.31)



Divyanshu Yadav
(99.28)



Piyush Tiwari
(99.26)



Alisha Verma
(99.23)



Avinash Kumar
(99.19)



Amisha Verma
(99.15)



Chetan Singh
(99.13)



Ritik Kumar
(99.13)



Shubham Kumar
(99.10)



Randheer
(99.08)



Aryansh Tripathi
(99.06)



Saurabh Maurya
(99.03)



Mohammad Afan
(99.03)



Pradumna Awasthi
(99.02)



Harsh
(99.02)



Abhay
(99.01)

**SCHOOL INTEGRATED
PROGRAM (SIP)**

Tradition of Gravity Continues,
Once Again Historical Result,
100% Students Cracked
JEE Main
(Based on Last Yr Cut off)

2020

80 Out of 80

Cracked JEE Main

We had three Batches
of 55, 15 and 10.

Many Top Ranks are
from these Batches

2019

79 Out of 80

50 Out of 79

in JEE Main in JEE Adv.

2018

83 Out of 85

62 Out of 83

in JEE Main in JEE Adv.

2017

80 Out of 85

63 Out of 80

in JEE Main in JEE Adv.

2016

39 Out of 40

31 Out of 39

in JEE Main in JEE Adv.

Selections Engineering 2019



194

AIR
(General)

Tarun



337

AIR
(General)

Aniket Agarwal



494

AIR
(General)

Shubh Sahu



497

AIR
(General)

Shlok Nemani

50 out of 79 Cracked JEE Advanced from SIP (School Integrated Program)

4 Ranks under 500 (General Category) | 2 Ranks under 10 (Reserved Category)

126 Selections in JEE Advanced | 61 Students above 99 Percentile in JEE Main 2019



Sanjana



Akash



Priyanka



Bibek Lakra



Neha Raj



Arindam

AIR - 3*

AIR - 4*

AIR - 68*

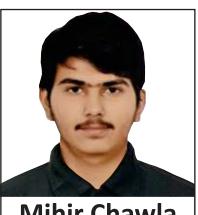
AIR - 150*

AIR - 177*

AIR - 809
(General EWS)



Priyam



Mihir Chawla



Madhur Kumar



Manish Kumar



Saumya Raj



Raghav

AIR - 1378
(General)

AIR - 2237
(General)

AIR - 2382
(General)

AIR - 2388
(General)

AIR - 2656
(General)

AIR - 2659
(General)



Ritveek



Vanshaj



Subir Gupta



Aryan Rastogi



Devansh



Abhisht Bose

AIR - 2709
(General)

AIR - 2787
(General)

AIR - 2881
(General)

AIR - 3167
(General)

AIR - 3600
(General)

AIR - 3784
(General)